mSSB UE2.3 Metabolic Engineering

Cellular metabolism and the main metabolic pathways

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Metabolite:

• a naturally occurring molecule typically under 1000 MW

Enzyme:

- any protein which catalyzes chemical reactions involving the small molecules
- (ribozyme = catalytic RNAs)

Transporter:

• a membrane bound protein which shuttles ions, small molecules or macromolecules across membranes, into cells or out of cells.

Metabolism:

- complete set of biochemical reactions within a cell
- sum of processes involved in energy conversions in the cell

Metabolic pathways

complex sequences of controlled chemical reactions



Metabolite:

• a naturally occurring molecule typically under 1000 MW

Background information from organic chemistry:

- Elements
- Bonds
- Molecules
- Isotopes
- lons
- Nomenclature
- Stereochemistry

Chemical components of a cell



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Catabolic and anabolic pathways in cellular metabolism



Classification of organisms

	Designation	Description
Source of Carbon	AutotrophHeterotroph	 CO₂ Organic molecules (e.g. sugars)
Source of Electrons	OrganotrophLithotroph	 Organic molecules (e.g. sugars) Inorganic molecules (e.g. H₂, H₂O, H₂S, NH₃, S)
Source of Energy	PhototrophChemotrophMixotroph	 Light Oxidation of chemical compounds Light & Oxidation of chemical compounds
Ability to use O ₂ for respiration & sensitivity to O ₂	 Strict/Obligate aerobe Strict/Obligate anaerobe Facultative aerobe/anaerobe Aerotolerant anaerobe 	 Require O₂ for respiration – cannot survive without O₂ Cannot survive in the presence of O₂ Can survive in the presence or absence of O₂ Do not respire O₂, but are able to survive in the presence of O₂

Human: Heterotroph, Organotroph, Chemotroph, Strict/Obligate aerobe *E. coli*: Heterotroph, Organotroph, Chemotroph, Facultative aerobe/anaerobe *S. cerevisiae*: Heterotroph, Organotroph, Chemotroph, Facultative aerobe/anaerobe Plants & algae: Autotroph, Lithotroph, Phototroph, Strict/Obligate aerobe

Different organisms – different cellular metabolisms



Cell content

	E. coli	S. cerevisiae	H. sapiens
Metabolites	3 755	16 042	114 100
Reactions	8 254	31 624	6 302
Pathways	1 336	9 595	49 029
Enzymes	1 204	909	2 126
Transporters	299	149	0
Proteins	1 549	1 259	5 779
Metabolite synonyms	37 982	27 947	333 312
Metabolites in reactions	3518 (93.7 %)	11 157 (69.5 %)	23 473 (20.6 %)
	http://www.ecmdb.ca	http://www.ymdb.ca	http://www.hmdb.ca
	Sajed et al. Nucleic Acids Research (2016) 44, D495-D501	Jewison et al. Nucleic Acids Research (2012) 40, D815-D820	Wishart et al. Nucleic Acids Research (2013) 41, D801-D807





Glycolysis



Glycolysis:

- Oxidation of 1 Glucose (6C) to 2 Pyruvate (3C)
- Production of cellular energy sources:

• 2 ATP

- 2 NADH,H⁺
- Supply of 6 precursor metabolites for biosynthesis
- ∆G'°= 74 kJ.mole⁻¹
- ΔG'= 98 kJ.mole⁻¹

Glycolysis



Pentose Phosphate pathway



ED pathway



Entner–Doudoroff Pathway:

- Only in some bacteria (ex. *E. coli*), archeae and *Entamoeba histolyca*, *Aspergillus niger, Penicillum notatum*
- Oxidation of 1 Glucose (6C) to 2 Pyruvate (3C)
- Production of cellular energy sources:
 - 1 ATP
 - 1 NADH,H⁺
 - 1 NADPH,H⁺
- Supply of 5 precursor metabolites for biosynthesis

ED pathway



Central pathways Metabolism of carbohydrates and carboxylic acids



Fermentation



ATP produced only by substrate-level phosphorylation

Fermentation



• ATP produced only by substrate-level phosphorylation

Krebs cycle



Krebs cycle



Respiration



External terminal electron acceptors:

Type of respiration	External terminal electron acceptors	Reduced products
Aerobic respiration	O ₂	H ₂ O
Anaerobic respiration	Fumarate: HOOC-CH=CH-COOH	Succinate: HOOC-CH ₂ -CH ₂ -COOH
	Trimethylamine N-oxide: $(CH_3)_3$ -N \rightarrow O	Trimethylamine: (CH ₃) ₃ -N
	S, S ₂ O ₃ ²⁻ , SO ₄ ²⁻	H ₂ S
	$NO_{3}^{-}, NO_{2}^{-}, NO$	N ₂
	Fe ³⁺	Fe ²⁺

- A H⁺ (electrochemical) gradient is produced across a membrane = proton-motrice force
- Flow of H⁺ down the gradient (across the membrane) through the H⁺ channel of ATP synthase: ATP synthesis = oxidative phosphorylation



- Cytoplasmic membrane
- Complexity ability to adapt to different
 - Growth conditions
 - Electron donors: NADH, NADPH, FADH₂, organic substances, H₂, NH₃, NO₂⁻, S, S²⁻, Fe²⁺
 - Electron acceptors:
 - organic compounds (fumarate, dimethyl sulfoxide, trimethylamine N-oxide)
 - inorganic compounds (O₂, NO₃⁻, NO₂⁻, NO, ClO₃⁻, ClO₄⁻, S, S₂O₃²⁻, SO₄²⁻, SeO₄²⁻, AsO₄³⁻, CO₂, oxidized manganese ions, gold, Fe³⁺)



E. coli aerobic respiration



Metabolism of carbohydrates and carboxylic acids

- Oxidation of 1 Glucose to
 - 6 CO₂ (Complete oxidation)
 - Various fermentation products (Partial oxidation)
- Production of cellular energy sources:
 - Up to 38 ATP / glucose
 - Reducing power (NADH, NADPH, ...)
- Tight regulation:
 - Redox potential
 - Energy charge
 - Presence of terminal e- acceptors
 - Growth substrate
 - Amount
 - Type
 - Catabolite repression
 - Diauxic growth: multiple carbon sources are utilized sequentially
 - Allosteric modulation of enzymes
 - Covalent modifications of enzymes (e.g. phosphorylation)
 - Transcriptional control
 - Compartmentalization & transport



Central pathways – Precursor metabolites – Building blocks

Metabolism of carbohydrates and carboxylic acids

- Supply of 12 major precursor metabolites for biosynthesis
 - Used with ATP and NAD(P)H for the biosynthesis of cellular building blocks

Precursor metabolites	Pathway	Amount required for biosynthesis of <i>E. coli</i>	Building blocks produced
Glucose-6-P	Glycolysis	205 µmol / g cell	NDP-glucose
Fructose-6-P	Glycolysis	71 µmol / g cell	NDP-mannose, NDP-N-acetylglucoseamine,
Glyceraldehyde-3-P Dihydroxyacetone-P	Glycolysis	129 µmol / g cell	Isoprenoids Glycerol-P (& lipids)
3-Phosphoglycerate	Glycolysis	1496 µmol / g cell	Gly, Ser, Cys, nucleotides (purine)
Phosphoenolpyruvate	Glycolysis	519 µmol / g cell	Phe, Tyr, Trp
Pyruvate	Glycolysis	2833 µmol / g cell	Ala, Val, Leu, Ile, Lys, Isoprenoids
Ribose-5-P	Pentose phosphate	898 µmol / g cell	His, nucleotides (pentose)
Erythrose-4-P	Pentose phosphate	361 µmol / g cell	Phe, Tyr, Trp
Acetyl-CoA	TCA cycle	3748 µmol / g cell	Leu, Fatty acids, Isoprenoids
α-Ketoglutarate	TCA cycle	1079 µmol / g cell	Glu, Gln, Pro, Arg, nucleotides (purine)
Oxaloacetate	TCA cycle	1787 µmol / g cell	Asp, Asn, Lys, Thr, Met, Ile, nucleotides
Succinyl-CoA	TCA cycle		Met, Lys, tetrapyrroles (ex. Heme)

Precursor metabolites – Building blocks – Macromolecules

Metabolism of carbohydrates and carboxylic acids

- Supply of 12 major precursor metabolites for biosynthesis
 - Used with ATP and NAD(P)H for the biosynthesis of cellular building blocks
 - Polymerization of building blocks



Isoprenoids / Terpenoids



Not essential for

- Growth
- Respiration
- Development
- Reproduction

Beneficial for the producer:

- Improve survival fitness
- Bactericides or fungicides
- Specific receptors

Produced at low titers

Complex organic compounds

- Difficult to synthetize
- Difficult to derivatize

Main classes

- Isoprenoids / Terpenoids
- Alkaloids
- Flavonoids
- Non ribosomal peptides
- Polyketides

Bioactive molecules

- Pharmaceuticals
 - Antibacterials
 - Antifungals
 - Antitumor
 - Antihelminthic
 - Antiviral
 - Herbicidal
 - Insecticidal
 - Immunosupressors

/

Interesting for humans

Candidates for metabolic engineering

Secondary metabolism

plants



Wilson & Roberts. Current Opinion in Biotechnology (2014) 26, 174–182

Secondary metabolism



Secondary metabolism

bacteria



Weissman & Leadlay. Nature Reviews Microbiology (2005) 3, 925-936

Producing sugars

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Producing sugars



Some invertebrates •

Glyoxylate by-pass:

•

•

- Glyoxysomes of eucaryotes •
- Allows grow on acetate and fatty acids: 2 Acetyl-CoA \rightarrow 1 Succinate •
- Supply of precursor metabolites for biosynthesis •

Producing sugars

- Autotroph organisms
 - CO₂ assimilation / CO₂ fixation / carbon fixation
- Phototroph
 - Energy = light

 $6 \text{ CO}_2 + 6 \text{ H}_2\text{O} \rightarrow \text{C}_6\text{H}_{12}\text{O}_6 + 6 \text{ O}_2$


Producing sugars

Light reactions

- e- flow: from H₂O to NADP⁺
- A H⁺ (electrochemical) gradient is produced across a membrane = proton-motrice force
- Flow of H⁺ down the gradient (across the membrane) through the H⁺ channel of ATP synthase: ATP synthesis = oxidative phosphorylation



Producing sugars

Calvin cycle



Producing sugars

Reverse/reductive TCA cycle

Arnon-Buchanan cycle:

- Used by some autotrophic anaerobic and microaerobic bacteria and archaea for CO₂ assimilation
- two ferredoxin-linked (Fd) CO₂-fixation reactions are O₂ sensitive



Ex. Chlorobium thiosulfatophilum

- Photosynthetic green sulfur bacterium
- Anaerobic
- Inorganic medium:
 - sulfide and thiosulfate as e- donors
 - CO₂ as an obligatory
 carbon source = Strictly
 autotrophic

Wood-Ljungdahl pathway:

- Used by some autotrophic anaerobic bacteria and archaea for CO₂ assimilation
 - Acetogenic bacteria
 - Methanogenic archeae
 - ...
- One $CO_2 \rightarrow CH_3$
- One $CO_2 \rightarrow CO$

- High energetic efficiency
- Limited to a few ecological niches
 - Anaerobiosis
 - Metals: Mo or W, Co, Ni, and Fe
 - Cofactors: tetrahydropterin and cobalamin



Fuchs-Holo bi-cycle

- Used only by green nonsulfur bacteria of Chloroflexaceae family
 - Phototroph, chemotroph & mixotroph
 - Autotroph & heterotroph
 - Anoxygenic
- Co-assimilation of CO₂ & numerous compounds (e.g., fermentation products) = mixotrophy
- High energy requirements
 - 7 ATP for Acetyl-CoA to Pyruvate
- No oxygen-sensitive steps



Berg. Applied and Environmental Microbiology (2011) 77, 1925-1936

Used only by the hyperthermophilic archaea of Crenarchaeota family

- dicarboxylate/4-hydroxybutyrate • (DC/HB) cycle
 - Desulfurococcales and Thermoproteales
 - Anaerobic ٠

•

- 3-hydroxypropionate/4hydroxybutyrate (HP/HB) cycle
 - Sulfolobales
 - Aerobic



Berg. Applied and Environmental Microbiology (2011) 77, 1925-1936

4-hydroxybutyrate cycles

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Transport & Metabolism: linked processes in the cell

Ex: the *lac* operon



Pierce. Genetics (2nd Ed.) Freeman & Co (2005)

Membranes:

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- Semi-permeable structure
- Dynamic
- Barrier with selective permeability
- Controlled entry & exit
 - Entry:
 - Nutriments
 - Signaling substances
 - Nucleic acids
 - Metal ions
 - Exit:
 - Products generated by metabolism
 - Secreted substances
 - Lipids
 - Carbohydrates
 - Proteins
 - Nucleic acids
 - Toxic substances
 - Metal ions
- Damaged \rightarrow cell death

- Phospholipid bilayer :
 - Esters of glycerol + fatty acids
 - + phosphate
 - Eukaryotes



- Bacteria
- Phospholipid monolayer :
 - Tetraethers of glycerol + fatty alcohols (+ phosphate esters)
 - Archaea



- Other lipids for rigidity
 - Sterols



- All eukaryotes Bacteria: methanotrophs
 - & mycoplasma
- Hopanes
 - Bacteria



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Transport across membranes

Eucaryotes



Transport classification: TC system

Passive transport:

- No energy required
- Occurs only in the downhill direction of concentration gradient



Facilitated diffusion:

http://www.tcdb.org

Transport classification: TC system

Active transport:

- Primary energy required
 - Chemical (ATP)
 - Electrical ٠
 - Solar •
- Occurs against a concentration gradient •

Group translocators:

substrate is modified during the transport process



TC#5: Transmembrane electron flow systems

http://www.tcdb.org

Kinetics of Transport processes

Movement of S_x is described by its flux JS_x :

- number of moles of S_x crossing a unit area of cell membrane per unit of time (moles.cm⁻²s⁻¹)
- Depends on :
 - permeability coefficient PS_X:
 - S_x solubility in lipids
 - S_x diffusion coefficient in lipids
 - Membrane thickness
 - Gradient across membrane
- Decomposed into:
 - Unidirectional influx $JS_X^{0 \rightarrow i}$ proportional to the outside concentration
 - Unidirectional efflux $JS_X^{i \rightarrow 0}$ proportional to the inside concentration
- at equilibrium $[S_X]_0 = [S_X]_i$ if S_x is not charged

If S_x is charged: voltage difference across membrane should be considered

Electrochemical energy: $\Delta \mu S_X = RT \ln ([S_X]_i / [S_X]_0) + z_XF (\Psi_i - \Psi_0)$

> F = Faraday constant = 96500 C $W_{-} = W_{-} = voltage difference across membra$

 $R = gas constant = 8,315 J.mol^{-1}K^{-1}$

T = temperature °K

 z_x = charge of S_x

 $\Psi_i - \Psi_0$ = voltage difference across membrane

Fick's Law: $JS_{X} = PS_{X} [S_{X}]_{0} - PS_{X} [S_{X}]_{i}$ influx efflux

Kinetics of Transport processes



Carrier mediated transport:

- Affinity
- Specificity
- Energy availability
- Regulation
- Localization

Major conformational changes

Steps: bind – transport – release ... like enzymes

Michaelis-Menten transport kinetics

$$V = V_{max} \frac{[S_X]_0}{K_m + [S_X]_0}$$

Different organisms – different cellular metabolisms



Cellular metabolism

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Metabolic pathways

• complex sequences of controlled chemical reactions



Cellular metabolism

Enzyme:

- Any protein which catalyzes chemical reactions involving the small molecules
- Catalysis = acceleration of chemical reactions useful time scale
- Efficiency
- Selectivity
- Specificity / Promiscuity
- Mild conditions of temperature and pH
- Regulation for coordination of different metabolic pathways



History:

- 1752: René Antoine Ferchault de Réaumur first recognition and description biological catalysis = digestion of meat by secretions of stomach
- 1877: Wilhelm Kühne first used the term enzyme = the unformed or not organized ferments, whose action can occur without the presence of organisms and outside of the same
- 1926: James B. Sumner showed that the enzyme urease was a pure protein
- 1982: Thomas R. Cech and Sidney Altma discovery of ribozymes (Nobel Prize in Chemistry 1989)

Enzymes

- Primary, secondary, tertiary, quaternary structure = essential for activity
- Some require post-translational modifications (phosphorylation, glycosylation, ...)
- Some require cofactors:
 - Inorganic ions: Na, K, Mg, Cu, Fe, Mn, Mo, Zn, Ni, Se, ...
 - Complex organic molecules = coenzymes

 Prostetic group = cofactor very tightly or even covalently bound

Coenzyme	Dietary precursor in mammals
Thiamine pyrophosphate	Vitamin B1 = thiamine
Flavin adenine dinucleotide (FAD)	Vitamin B2 = riboflavin
Nicotinamide ademine dinucleotide (NAD)	Vitamin B3 = nicotinic acid (niacin)
Coenzyme A	Vitamin B5 = panthothenic acid
Pyridoxal phosphate	Vitamin B6 = pyridoxine
Biocytin	Vitamin B8 (H) = biotin
Tetrahydropholate	Vitamin B9 (M) = folic acid
5'deoxyadenosylcobalamin	Vitamin B12 = cobalamin
Ascorbate	Vitamin C = ascorbic acid
Menaquinone	Vitamin K
Lipoate	Not required in diet
Coenzyme Q	Not required in diet



- EC X.Y.Z.W X = class
 - Y = subclass
 - Z = sub-subclass
 - W = the serial number of the enzyme in its sub-subclass

n°	Class	Type of reaction catalyzed
EC 1	Oxidoreductases 🍟 + 🔛 🛹 🔲 + ビ	Transfer of e- = oxidation/reduction reactions
EC 2	Transferases + + +	Transfer of a functional group (e.g. methyl, glycosyl or phosphate group)
EC 3	Hydrolases 🛛 🗧 + 🐣 귍 📋 + 🤜	Hydrolysis of various bonds
EC 4	Lyases 🛛 🕹 📥 + 🗖	Cleavage of various bonds by means other than hydrolysis and oxidation
EC 5	Isomerases	Isomerization changes within a single molecule
EC 6	Ligases $ + + + + + + + $	Formation of covalent bonds coupled with the hydrolysis of a diphosphate bond in NTP
EC 7	Translocases	Movement of ions / molecules across membranes or their separation within membranes

How enzymes work?

- Create an energetically favorable environment for the reaction to take place
- Active site



 $R = gas constant = 8,315 J.mol^{-1}K^{-1}$

T = temperature °K

Enzymes do not change

- K′_{eq}
- ΔG′°
- ΔG'

Free energy

ΔG'° are additive	For redox reactions: standard reduction potential E'° is used to calculate $\Delta G'^{\circ}$
$A \equiv B \Delta G'^{\circ}_{1}$	A + 2 e- + 2 H ⁺ <i>ح</i> AH ₂ E'° _A
$B \longrightarrow C \Delta G'^{\circ}_{2}$	BH ₂ \implies B + 2 e- + 2 H ⁺ -E'° _B
$A \longrightarrow C \Delta G'^{\circ} = \Delta G'^{\circ}_{1} + \Delta G'^{\circ}_{2}$	$A + BH_2 \longrightarrow AH_2 + B \qquad \Delta E'^{\circ} = E'^{\circ}_A - E'^{\circ}_B$
	$\Delta G'^{\circ} = - nF \Delta E'^{\circ}$ n = number of e- transferred F = Faraday constant = 96500 C

Actual free energy of a reaction changes depends on reactant and product concentrations

$aA + bB $ $cC + dD$ $\Delta G' = \Delta G'^{\circ} + RT ln Q$	$Q = \frac{[C]^{a} [D]^{a}}{[A]^{a} [B]^{b}} = reaction quotient$
----------------------------------------------------------------	-------------------------------------------------------------------

∆G'	Reaction	
< 0	Proceeds spontaneously forward	Exergonic
= 0	Is at equilibrium	
> 0	Cannot occur spontaneously – an input of free energy is required Proceeds spontaneously in reverse	Endergonic

Glycolysis Glucose	5000 μM	∆G′° (kJ.mol⁻¹)	∆G' (kJ.mol⁻¹)	
AIP		-16.7	-34	
Glucose-6-P	83 µM		\uparrow	
\bigstar		1.67	-2.9	
Fructose-6-P	14 μM			
ATP		-14.2	-19	
Fructose-1,6-bisP	31 µM		$\overline{\mathbf{x}}$	lanza nazativa fraz
^ ´		23.9	-0.23	large negative free
Dihydroxyacetone-P Glyceraldehyde-3-P	140uM 19 uN	vi 7.56	2.4	energy changes =
NAD+		6.3	-1.29	thormodynamically
1.3-bisphosphoglycerate	1 uM			irrovorsiblo
ADP		-18 9	0.09	IIIEVEISIDIE
3-nhosnhoglycerate	120 uM	10.5		
	120 μινι	лл	0.83	No reaction is at
	20	4.4	0.83	equilibrium
	50 μινι	1 0	11	
Dhasabaaaalay <i>iriyya</i> ta	22	1.0	1.1	Concentrations are
ADP	23 μινι	04 -	¥	at steady state
ATP		-31.7	-23	
Pyruvate	51 μM			
		TOTAL:	TOTAL:	
	ΔΠΡ: 1650 μΙΜ	-73.97	-98.27	
	Pi: 1000 μM			

Free energy changes over reactions of Glycolysis in erythrocytes

How enzymes work?

- Create an energetically favorable environment for the reaction to take place
- Lower the activation energy
- Enzymes do not change
 - Reaction equilibrium (K'_{eq})
 - Thermodynamic feasibility of the reaction ($\Delta G'$)
- Enhance reaction rate (velocity)

reaction rate = $\frac{d[P]}{dt}$

Reaction rate is proportional

- Concentration of substrates (reactants)
- Rate constant k



- the amount of product formed increases with time
- a time is reached when there is no net change in the concentration of S or P
- the enzyme is still actively converting S into P and visa versa, but the reaction equilibrium has been attained



 the initial velocity (V₀) for each substrate concentration is determined from the slope of the curve at the beginning of a reaction, when the reverse reaction is insignificant

= Simplifying approach

Initial velocity represents best the enzyme activity – no factors that can decrease it:

- Inhibition products
- pH changes
- Denaturation of enzyme

Initial Velocity

Steady-state

- Pre-Steady state: very short to be observed
- Steady state:
 - [ES] constant
 - V₀ reflects the steady state = approximation







- simple model that accounts for most of the features of enzyme catalyzed reactions
- Postulation of the reversible formation of ES







 $E + S \longrightarrow ES \longrightarrow EP \longrightarrow E + P$





Changes in the Concentration of Reaction Participants = formation rates – breakdown rates

Rate of [S] evolution =
$$\frac{d[S]}{dt}$$
 = $-k_1$ [E] [S] + k_1 [ES]

Rate of [E] evolution =
$$\frac{d[E]}{dt} = -k_1 [E] [S] + k_1 [ES] + k_2 [ES] - k_2 [P] [E]$$

Rate of [ES] evolution =
$$\frac{d[ES]}{dt} = k_1 [E] [S] - k_1 [ES] - k_2 [ES] + k_2 [P] [E]$$

Rate of [P] evolution =
$$\frac{d[P]}{dt} = k_2 [ES] - k_2 [P] [E]$$

= reaction rate



Changes in the Concentration of Reaction Participants = formation rates – breakdown rates

Rate of [S] evolution =
$$\frac{d[S]}{dt} = -k_1 [E] [S] + k_{-1} [ES]$$

Rate of [E] evolution = $\frac{d[E]}{dt} = -k_1 [E] [S] + k_{-1} [ES] + k_2 [ES]$
Rate of [ES] evolution = $\frac{d[ES]}{dt} = k_1 [E] [S] - k_{-1} [ES] - k_2 [ES]$
Rate of [P] evolution = $\frac{d[P]}{dt} = k_2 [ES]$
= reaction rate = V₀

1st assumption: initial rate [P] ≅ 0 k_{-2} [P] [E] ≅ 0



Changes in the Concentration of Reaction Participants = formation rates – breakdown rates

Rate of [S] evolution =
$$\frac{d[S]}{dt} = -k_1 [E] [S] + k_{-1} [ES]$$

Rate of [E] evolution = $\frac{d[E]}{dt} = -k_1 [E] [S] + k_{-1} [ES] + k_2 [ES]$
Rate of [ES] evolution = $\frac{d[ES]}{dt} = k_1 [E] [S] - k_{-1} [ES] - k_2 [ES] = 0$
Rate of [P] evolution = $\frac{d[P]}{dt} = k_2 [ES]$
= reaction rate = V₀

 2^{nd} assumption: steady state [ES] ≅ constant $\frac{d[ES]}{dt} = 0$ 66





$$V_0 = V_{max} \frac{[S_0]}{K_m + [S_0]}$$

 $V_{max} = k_{cat} [E_t]$

 If [S] >> K_m : the rate of product formation is maximum

$$\frac{d[\mathsf{P}]}{dt} = \mathsf{V}_{\max} = k_{cat} \,[\mathsf{E}_{\mathsf{t}}]$$

• If [S] = K_m : the rate of product formation is half of the maximum

$$\frac{d[P]}{dt} = \frac{V_{max}}{2} = \frac{k_{cat} [E_t]}{2}$$

• If [S] << K_m : the rate of product formation depends on both [E] \cong [E_t] and [S] through the efficiency constant k_{cat}/K_m

$$\frac{d[P]}{dt} = V_{max} \frac{[S]}{K_{m}} = [E_{t}] [S] \frac{k_{cat}}{K_{m}}$$



One substrate – one product

• EC 5: isomerases





One substrate – 2 products

- EC 3: hydrolases
- EC 4: lyases

$$E + S \underset{k_{-1}}{\overset{k_{1}}{\longrightarrow}} ES \underset{k_{-2}}{\overset{k_{2}}{\longrightarrow}} EPQ \underset{k_{-2}}{\overset{k_{2}}{\longrightarrow}} EQ + P \underset{k_{-3}}{\overset{k_{-3}}{\longrightarrow}} E + P + Q$$

$$V_{0} = [E_{t}] \frac{k_{2}k_{3}}{k_{2} + k_{3}} \frac{[S_{0}]}{[S_{0}] + \frac{k_{-1}k_{3}(k_{-1} + k_{2})}{k_{1}^{2}(k_{2} + k_{3})}}$$

2 substrates – 2 products

A + B 🔁 P + Q

- EC 1: oxidoreductases
- EC 2: transferases

Sequential Mechanisms



$$V_{0} = [E_{t}] \frac{k_{3} k_{4}}{k_{3} + k_{4}} \frac{[A] [B]}{[A] [B] + [B] \frac{k_{3} k_{4}}{k_{1} (k_{3} + k_{4})}} + [A] \frac{k_{4} (k_{-2} + k_{3})}{k_{2} (k_{3} + k_{4})} + \frac{k_{-1} k_{4} (k_{-2} + k_{3})}{k_{1} k_{2} (k_{3} + k_{4})}$$

Second order reactions

2 substrates – 2 products

A + B 🗾 P + Q

• EC 1: oxidoreductases

• EC 2: transferases

Ping-Pong Mechanisms



2 substrates – 2 products

A + B **~** P + Q

Ping-Pong Mechanisms

EC 2.6.1.1 Glutamate aspartate aminotransferase

L-glutamate + oxaloacetate ↔ 2-oxoglutarate + L-aspartate


Michaelis-Menten Kinetics

Third order reactions

3 substrates – n products

A + B + C **P** + Q + ...

• EC 1: oxidoreductases

- EC 2: transferases
- EC 6: ligases

Many possibilities & combinations:

- Sequential Mechanisms
 - Random
 - Ordered
- Ping-Pong Mechanisms

Ex. ordered ter-ter mechanism: EC 6.2.1.4 succinyl-CoA synthetase

succinyl-CoA + GDP + Pi \leftrightarrow succinate + GTP + CoA-SH В Α С R Q Ρ GDP succinyl-CoA Pi CoA-SH succinate GTP Α В Ρ Q R *k*_1 *k*_5 *k*_3 k_2 k_{22} k_3 k₄ k₋₄ *k*_6 k_{5} Ε EA EAB EABC EPQR EQR ER Ε

Michaelis-Menten Kinetics

Third order reactions

3 substrates – n products

A + B + C **P** + Q + ...

• EC 1: oxidoreductases

- EC 2: transferases
- EC 6: ligases

Many possibilities & combinations:

- Sequential Mechanisms
 - Random
 - Ordered
- Ping-Pong Mechanisms

Ex. Ping-pong mechanism: EC 1.2.1.12 glyceraldehyde-3-P dehydrogenase

glyceraldehyde-3-P + NAD⁺ + Pi \leftrightarrow 1,3-diphosphoglycerate + NADH,H⁺ В С Α Q Ρ glyceraldehyde-3-P NADH,H⁺ NAD^+ 1,3-diphosphoglycerate Pi В Ρ Α k_2 *k*_2 k_3 k_{-3} k₋₄ *k*_5 ΕA EAB FPB FB FAB FABC EAO ΕA

Effect of Various Types of Inhibitors

None $V = V_{max} [S]/([S] + K_m)$ K_m V_{max} Competitive $V = V_{max} [S]/([S] + K_m (1 + [I]/K_i))$ $K_m (1 + [I]/K_i)$ V_{max} Noncompetitive $V = V_{max} [S]/((1 + [I]/K_i) ([S] + K_m))$ K_m $V_{max}/(1 + [I]/K_i)$ Uncompetitive $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max}/(1 + [I]/K_i')$ Mixed $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max}/(1 + [I]/K_i')$ $E + S$ K_1 ES K_2 $E + P$ $-none$ $Competitive$ $Noncompetitive$ $Noncompetitive$ $Noncompetitive$ $E + I$ K_3 EI $K_i = \frac{[E] [I]}{[EI]}$ $Mixed$ $ES + I$ K_3 EIS $K_i' = \frac{[ES] [I]}{[EIS]}$	Inhibition Type	Rate Equation	Apparent Km	Apparent V _{max}
Competitive $V = V_{max} [S]/([S] + K_m (1 + [I]/K_i))$ $K_m (1 + [I]/K_i)$ V_{max} Noncompetitive $V = V_{max} [S]/((1 + [I]/K_i) ([S] + K_m))$ K_m $V_{max} / (1 + [I]/K_i)$ Uncompetitive $V = V_{max} [S]/((1 + [I]/K_i))$ $K_m / (1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i)$ Mixed $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i')$ $E + S \rightleftharpoons_{k_1} ES \rightleftarrows_{k_2} E + P$ -noneCompetitive $V = V_{max} [S]/(I + [I]/K_i) K_m + (1 + [I] K_i' [S])$ Noncompetitive $Uncompetitive$ Noncompetitive $K_1 = ES \rightleftarrows_{k_2} E + P$ -Noncompetitive $Wixed$ -Noncompetitive $E + I \rightleftarrows_{k_3} EI$ $K_i = \frac{[E] [I]}{[EI]}$ $ES + I \rightleftarrows_{k_3} EIS$ $K_i' = \frac{[ES] [I]}{[EIS]}$	None	$V = V_{max} [S]/([S] + K_m)$	K _m	V _{max}
Noncompetitive $V = V_{max} [S]/((1 + [I]/K_i) ([S] + K_m)))$ K_m $V_{max} / (1 + [I]/K_i)$ Uncompetitive $V = V_{max} [S]/(K_m + [S] (1 + [I]/K_i')))$ $K_m / (1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i')$ Mixed $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i')$ $E + S \rightleftharpoons_{k_1} ES \xleftarrow_{k_2} E + P$ -none-competitiveNoncompetitive-none-competitive V_{max} $K_i = \frac{[E] [I]}{[EI]}$ Mixed $E + I \rightleftharpoons_{k_3} EI$ $K_i = \frac{[E] [I]}{[EI]}$ Mixed $ES + I \rightleftharpoons_{k_3} EIS$ $K_i' = \frac{[ES] [I]}{[EIS]}$	Competitive	$V = V_{max} [S]/([S] + K_m (1 + [I]/K_i))$	$K_{m} (1 + [I]/K_{i})$	V _{max}
Uncompetitive $V = V_{max} [S]/(K_m + [S] (1 + [I]/K_i'))$ $K_m / (1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i')$ Mixed $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max} / (1 + [I]/K_i')$ $E + S \stackrel{k_1}{\underset{k_3}{\underset{k_3}{\underset{k_3}{\atop{k_3}}}} EI \qquad K_i = \frac{[E] [I]}{[EI]}$ none Competitive Uncompetitive Mixed $ES + I \stackrel{k_3}{\underset{k_3}{\underset{k_3}{\atop{k_3}}} EIS \qquad K_i' = \frac{[ES] [I]}{[EIS]}$	Noncompetitive	$V = V_{max} [S]/((1 + [I]/K_i) ([S] + K_m))$	K _m	$V_{max} / (1 + [I]/K_i)$
Mixed $V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S]))$ $K_m (1 + [I]/K_i)/(1 + [I]/K_i')$ $V_{max}/(1 + [I]/K_i')$ $E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$ $E + I \xrightarrow{k_3} EI$ $K_i = \frac{[E] [I]}{[EI]}$ $ES + I \xrightarrow{k_3} EIS$ $K_i' = \frac{[ES] [I]}{[EIS]}$	Uncompetitive	$V = V_{max} [S]/(K_m + [S] (1 + [I]/K_i'))$	$K_{\rm m} / (1 + [I] / K_{\rm i}')$	$V_{max}/(1 + [I]/K_i')$
$E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$ $= -none$ $= Competitive$ $= Noncompetitive$ $= 0 Noncompetit$	Mixed	$V = V_{max} [S]/((1 + [I]/K_i) K_m + (1 + [I] K_i' [S])$	$K_{m} (1 + [I]/K_{i})/(1 + [I]/K_{i}')$	$V_{max} / (1 + [I]/K_i')$
$ES + I \xrightarrow{k_3} EIS \qquad K_i' = \frac{[ES][I]}{[EIS]}$	$E + S \stackrel{k_1}{\underset{k_{-1}}{\longrightarrow}} ES$ $E + I \stackrel{k_3}{\underset{k_{-3}}{\longrightarrow}} EI$	$E + P$ $K_{i} = \frac{[E][1]}{[EI]}$	 none Competitive Noncompetitive Uncompetitive Mixed 	
	$ES + I \rightleftharpoons_{k_{-3}}^{k_3} E$	$K_i' = \frac{[ES][I]}{[EIS]}$		

Non Michaelis-Menten Kinetics enzymes

- Enzymes that regulate the metabolism = regulatory enzymes
- Display increased or decreased activity in response to certain signals
- At key point on the metabolic map
 - At the start of metabolic pathways
 - At junctions between metabolic pathways
 - Control rates
 - Channel metabolites

Allosteric enzymes

- Reversible & Non-covalent binding of regulatory compounds
- Homotropic:
 - modulator = substrate
- Heterotropic:
 - modulator ≠ substrate
 - = allosteric modulator
 - binds at sites different than the active site
- Conformational changes
- Large proteins
- Multimeric protein (often)

Covalently modulated enzymes

- Reversible & covalent modification by other enzymes
 - Phosphorylation
 - Methylation
 - Adenylation
 - Ribosylation
 - •
- Irreversible & covalent modification by other enzymes
 - Proteolysis

Other mechanisms

- Interaction with regulatory proteins
- Degradation

Allosteric enzymes

Cooperative behavior = binding of a certain ligand influences the affinity of the protein to a further ligand of the same (homotropic) or another type (heterotropic)



Non Michaelis-Menten Kinetics enzymes



Kinetic parameters of enzymes



- enzymes operating in secondary metabolism are, on average, ~30-fold slower than those of central metabolism
- Substrate low molecular mass and hydrophobicity appear to limit K_{M} optimization

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